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|--------------------------|--|--------------------------------|------------------|
| <b>Date</b>              | <b>Fall 2015-2016</b>                      | <b>Credits</b>                 | <b>3 credits</b> |
| <b>Course Title</b>      | Advanced Topics in Engineering Mathematics | <b>Course Number</b>           | <b>Math 501</b>  |
| <b>Pre-requisite (s)</b> | <b>None</b>                                | <b>Co-requisite (s)</b>        | <b>None</b>      |
| <b>Hours</b>             | <b>36</b>                                  | <b>Out of Class Work Hours</b> | <b>90</b>        |

### Place and Time of Class Meeting

Tuesday 13:00-15:50 @ D304

### Name and Contact Information of Instructor

Prof. Dr. Veli Shahmurov  
 Phone: +90 216 6771630- ext. 2422  
 E-mail: veli.sahmurov@okan.edu.tr

### Book required

- 1.Veli Shakhmurov and G. Uzgoren, Linear Algebra and applications, Okan University, 2014;
2. Walter Rudin, *Functional Analysis*, 2nd Edition, McGraw Hill, 1991;
3. Marsel B. Finan, A first course in quasilinear partial differential equations for physical and engineering, ArkansasTech University, 2016

### Classroom expectations for students

#### Attendance Policy

Students are liable to attend every course, practical and laboratory work of the program they are enrolled and to take the exams and participate in academic work required for achieving the course. Student attendance to all courses is compulsory. Students who do not attend a minimum 70% of the theoretical courses and 80% of the practical courses will be considered as absent for the related courses. Students who do not meet the mandatory minimum requirement of attendance will fail the course. Students who fail a course for not fulfilling minimum attendance requirement are obliged to meet the attendance requirement when they re-take the course.

#### Student Tardiness Policy

Students are permitted to arrive to the class in the first 15 minutes after the scheduled start of the course; extension of tardiness time is in instructor's discretion.

### Course Description (must correspond exactly to Catalog description)

The purpose of this course is to prepare students first of all background of functional analysis, i.e. linear spaces and normed spaces, linear operators in normed spaces, linear functional, regular generalized functions, singular generalized functions, Fourier series and Fourier integrals, Fourier transformations, Laplace transformations. Then application of functional analysis to Mathematical Physics equations occur in the engineering problems, i.e. boundary and initial value problems, fundamental solutions of PDE, elliptic equations, parabolic equations, hyperbolic equations, wave equations, Schrödinger equations, eigen value problems, nonlinear differential equations

### Learning Objectives

At the end of this course the student will be able to:

- To recognize and identify linear spaces, particularly vector spaces and function spaces;
- To study linear operators in linear and normed spaces and properties of differential operators;
- To treat linear functional and its properties, Hahn-Banach theorem and its applications;
- To study regular generalized functions and its representation with local integrable functions;
- To analyze singular generalized functions and distinguish with regular generalized functions;
- To study Fourier series and Fourier integrals, Fourier transformations applications to differential equations;
- To study Laplace transformations and applications to initial value problems for differential equations;
- To ascertain boundary and initial value problems for ordinary differential equations;
- To study the classification of partial differential equations of the second order;
- Find the fundamental solutions of some partial differential equations;
- fundamental solutions of elliptic equations of the second order;
- fundamental solutions of hyperbolic equations of the second order;
- fundamental solutions of parabolic equations of the second order
- To ascertain the boundary value problems for elliptic equations;
- To ascertain the initial value and mixed value problems for hyperbolic equations;
- To study the initial value and mixed value problems for parabolic equations;
- To study Schrödinger equations in different domains
- To treat Eigen value problems for elliptic equations and its properties;
- To study the nonlinear partial differential equations and its applications in physics and engineering.

**Topical Outline and Schedule**

| <b>DATE</b>                         |  | <b>WEEK 1</b>  |  |
|-------------------------------------|--|--|--|
| <b>SPECIFIC OBJECTIVES</b>          |  | <ul style="list-style-type: none"> <li>• Introduce the course to the students</li> <li>• To show that the set of real and complex numbers are linear spaces</li> <li>• Investigate multivariable functions acting in real and complex domains</li> </ul>   |  |
| <b>TOPIC (S)</b>                    |  | <ul style="list-style-type: none"> <li>• Syllabus</li> <li>• Linear spaces, vector and function spaces</li> <li>• The spaces with dot products and properties</li> <li>• <math>L^2</math> and <math>l^2</math> spaces and its properties</li> <li>• Discuss Course Outline, Instructor to verify completion</li> </ul>       |  |
| <b>LEARNING ACTIVITIES</b>          |  | Discussion of Syllabus<br>Completion of exercises and problems   |  |
| <b>OUT OF CLASS WORK ASSIGNMENT</b> |  | Review the Syllabus<br><br>Homework 1: To read the concept of multivariable analysis   |  |
| <b>DATE</b>                         |  | <b>WEEK 2</b>  |  |
| <b>SPECIFIC OBJECTIVES</b>          |  | To show that the function space $L_p$ and the sequence space $l_p$ are linear and normed;<br>To prove that $H^2$ and $W^{2,p}$ spaces are normed and Banach spaces   |  |
| <b>TOPIC (S)</b>                    |  | <ul style="list-style-type: none"> <li>• Normed spaces, Banach spaces and examples</li> <li>• <math>L_p</math> and <math>l_p</math> spaces and its properties</li> <li>• Hölder and Sobolev spaces and embedding theorems</li> <li>•</li> <li>•</li> </ul>   |  |
| <b>LEARNING ACTIVITIES</b>          |  | Discussion of MOS transistor   |  |
| <b>OUT OF CLASS WORK ASSIGNMENT</b> |  | Homework 2: To show that Sobolev spaces are Banach spaces  |  |
| <b>DATE</b>                         |  | <b>WEEK 3</b>  |  |
| <b>SPECIFIC OBJECTIVES</b>          |  | <ul style="list-style-type: none"> <li>• To show different examples for linear functional in the class of continuous functions</li> <li>• To show examples for linear operators in the class of differentiable functions</li> <li>• To show examples for linear operators and functional in the space of sequence</li> </ul> |  |
| <b>TOPIC (S)</b>                    |  | <ul style="list-style-type: none"> <li>• Linear operators in normed spaces and its properties</li> </ul>   |  |

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|                                     | <ul style="list-style-type: none"> <li>Linear differential operators;</li> <li>Linear functional in normed spaces and its properties</li> </ul>  |
| <b>LEARNING ACTIVITIES</b>          | <p>Discussion of single stage amplifier</p> <p>Discussion of common source amplifier</p>   |
| <b>OUT OF CLASS WORK ASSIGNMENT</b> | Homework 3: To prove that different differential operators are linear  |
| <b>DATE</b>                         | <b>WEEK 4</b>  |
| <b>SPECIFIC OBJECTIVES</b>          | <ul style="list-style-type: none"> <li>To show class of differentiable finite functions</li> <li>Analyze the class of local integrable functions</li> <li>Investigate Delta function and its properties</li> <li>Show examples on regular generalized functions</li> </ul> |
| <b>TOPIC (S)</b>                    | <ul style="list-style-type: none"> <li>Regular generalized functions and its representation with local integrable functions;</li> <li>Singular generalized functions and distinguish with regular generalized functions</li> </ul>   |
| <b>LEARNING ACTIVITIES</b>          | <p>Illustrate examples on class of differentiable functions</p> <p>Discussion of singular generalized functions</p> <p>Completion of exercises and problems</p>  |
| <b>OUT OF CLASS WORK ASSIGNMENT</b> | Homework 4: analyze of regular and singular generalized functions in class of continuous differentiable functions  |
| <b>DATE</b>                         | <b>WEEK 5</b>  |
| <b>SPECIFIC OBJECTIVES</b>          | <ul style="list-style-type: none"> <li>To study Fourier series in Hilbert spaces</li> <li>To study Fourier integrals in class of periodic functions</li> <li>Application of Fourier transforms to differential equations;</li> </ul>                                       |
| <b>TOPIC (S)</b>                    |  |
| <b>LEARNING ACTIVITIES</b>          | <p>The Fourier series;</p> <p>The Fourier integrals;</p> <p>The Fourier transforms</p>   |
| <b>OUT OF CLASS WORK ASSIGNMENT</b> | Homework 5: Fourier series of trigonometric systems  |
| <b>DATE</b>                         | <b>WEEK 6</b>  |
| <b>SPECIFIC OBJECTIVES</b>          | <ul style="list-style-type: none"> <li>To study Laplace transformations and its properties;</li> <li>Application of the Laplace transform to initial value problems for differential equations</li> <li></li> </ul>  |

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|                                     | •   |
| <b>TOPIC (S)</b>                    | • Single ended Operational Amplifiers   |
| <b>LEARNING ACTIVITIES</b>          | Laplace transforms and applications   |
| <b>OUT OF CLASS WORK ASSIGNMENT</b> | Homework 6: Application of the Laplace transform to differential equations  |
| <b>DATE</b>                         | <b>WEEK 7</b>   |
| <b>SPECIFIC OBJECTIVES</b>          | <ul style="list-style-type: none"> <li>• Analysis of local and nonlocal boundary value problems for ordinary differential equations of the second order;</li> <li>• Initial value problems for ordinary differential equations</li> </ul>                     |
| <b>TOPIC (S)</b>                    | <ul style="list-style-type: none"> <li>• Boundary value problems for ordinary differential equations</li> <li>• Initial value problems for ordinary differential equations</li> </ul>   |
| <b>LEARNING ACTIVITIES</b>          |   |
| <b>OUT OF CLASS WORK ASSIGNMENT</b> | <ul style="list-style-type: none"> <li>• Continue research on boundary and initial value problems for ordinary differential equations</li> </ul> <p>Homework 7: Solve problems on boundary and initial value problems for ordinary differential equations</p> |
| <b>DATE</b>                         | <b>WEEK 8</b>   |
| <b>SPECIFIC OBJECTIVES</b>          | <ul style="list-style-type: none"> <li>• Identify elliptic equations of the second order;</li> <li>• Analyze of hyperbolic equations of the second order;</li> <li>• Study the parabolic equations</li> </ul>   |
| <b>TOPIC (S)</b>                    | • The classification of partial differential equations of the second order  |
| <b>LEARNING ACTIVITIES</b>          | Discussion of partial differential equations of second order  |
| <b>OUT OF CLASS WORK ASSIGNMENT</b> | <p>Continue research and work on final project</p> <p>Homework 8: The classification of different partial differential equations of the second order</p>  |
| <b>DATE</b>                         | <b>WEEK 9</b>   |
| <b>SPECIFIC OBJECTIVES</b>          | • Evaluate students via midterm exam  |
| <b>TOPIC (S)</b>                    | • Midterm Exam  |
| <b>LEARNING ACTIVITIES</b>          | None  |
| <b>OUT OF CLASS WORK</b>            | None  |

| ASSIGNMENT                          |   |
|-------------------------------------|---|
| WEEK 10                             |   |
| <b>SPECIFIC OBJECTIVES</b>          | <ul style="list-style-type: none"> <li>Identify the fundamental solutions of elliptic equations of the second order;</li> <li>Analyze fundamental solutions of hyperbolic equations of the second order;</li> <li>Find fundamental solutions of parabolic equations of the second order;</li> </ul>   |
| <b>TOPIC (S)</b>                    | <ul style="list-style-type: none"> <li>Fundamental solutions of partial differential equations</li> </ul>   |
| <b>LEARNING ACTIVITIES</b>          | Discussion of partial differential equations  |
| <b>OUT OF CLASS WORK ASSIGNMENT</b> | Homework 10: Finds fundamental solutions of different type partial differential equations   |
| WEEK 11                             |   |
| <b>SPECIFIC OBJECTIVES</b>          | <ul style="list-style-type: none"> <li>Find eigen value of boundary value problems for Laplace equations</li> <li>Identify eigen functions of boundary value problems for Laplace equations</li> <li>Analyze local and nonlocal value of boundary value problems for elliptic equations</li> </ul>  |
| <b>TOPIC (S)</b>                    | <ul style="list-style-type: none"> <li>The boundary value problems for elliptic equations;</li> <li>Local and nonlocal boundary conditions</li> </ul>   |
| <b>LEARNING ACTIVITIES</b>          | Discussion of local and nonlocal boundary value problems<br>Discussion of eigen value and eigen functions of elliptic operators   |
| <b>OUT OF CLASS WORK ASSIGNMENT</b> | Homework 11: Finds eigen value and eigen functions of local boundary value problems for the Laplace equation  |
| WEEK 12                             |   |
| <b>SPECIFIC OBJECTIVES</b>          | <ul style="list-style-type: none"> <li>Identify the initial value problems for the wave equations</li> <li>Analyze the mixed value problems for the wave equations</li> <li>Finds the solution of the initial value problems for the wave equations</li> <li>Finds the solution of the mixed value problems for the wave equations</li> </ul> |
| <b>TOPIC (S)</b>                    | <ul style="list-style-type: none"> <li>The initial value and mixed problems for hyperbolic equations</li> </ul>   |
| <b>LEARNING ACTIVITIES</b>          | Discussion of the initial and mixed value value problems for the wave equations   |
| <b>OUT OF CLASS</b>                 | Homework 12: Finds the solution of the initial value problems for the different type wave equations   |

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| <b>WORK ASSIGNMENT</b>              | Doing homework 12   |
| <b>DATE</b>                         | <b>WEEK 13</b>  |
| <b>SPECIFIC OBJECTIVES</b>          | <ul style="list-style-type: none"> <li>Identify initial value problems for the heat equations;</li> <li>Analyze mixed value problems for the heat equations;</li> <li>Find the solution of initial value problems for the heat equations</li> </ul>                         |
| <b>TOPIC (S)</b>                    | <ul style="list-style-type: none"> <li>The initial value and mixed value problems for parabolic equations</li> </ul>  |
| <b>LEARNING ACTIVITIES</b>          | Discussion of initial value and mixed value problems for the parabolic equations of second order  |
| <b>OUT OF CLASS WORK ASSIGNMENT</b> | Homework 13: Finds the solution of the initial value problems for the different type parabolic equations  |
| <b>DATE</b>                         | <b>WEEK 14</b>  |
| <b>SPECIFIC OBJECTIVES</b>          | <ul style="list-style-type: none"> <li>To study Schrödinger equations in all spaces;</li> <li>Identify Schrödinger equations in half spaces</li> <li>Analyze Schrödinger equations in bounded domains</li> </ul>  |
| <b>TOPIC (S)</b>                    | <ul style="list-style-type: none"> <li>Schrödinger equations in considered on different domains</li> <li>Eigen value and Eigen spaces of Schrödinger operators</li> </ul>   |
| <b>LEARNING ACTIVITIES</b>          | <ul style="list-style-type: none"> <li>Discussion of Eigen value and Eigen spaces of Schrödinger operators</li> </ul>   |
| <b>OUT OF CLASS WORK ASSIGNMENT</b> | Homework 14: Finds the solutions of Schrödinger equations defined on all spaces   |
| <b>DATE</b>                         | <b>WEEK 15</b>  |
| <b>SPECIFIC OBJECTIVES</b>          | <ul style="list-style-type: none"> <li>To treat boundary value problems for nonlinear elliptic equations;</li> <li>Analyze initial value problems for nonlinear hyperbolic equations;</li> <li>To study initial value problems for nonlinear parabolic equations</li> </ul> |
| <b>TOPIC (S)</b>                    | <ul style="list-style-type: none"> <li>The nonlinear partial differential equations and its properties</li> </ul>   |
| <b>LEARNING ACTIVITIES</b>          | Elliptic equations  |
| <b>OUT OF CLASS WORK ASSIGNMENT</b> | Homework 15: Finds the solutions of nonlinear partial differential equations.   |
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### Instructional Methods

In developing methodological strategies, it is best to discuss them between teachers and students in an environment of freedom and mutual agreement in order to ensure that the students make them their own and take responsibility for their execution and for attaining the goals of this course.

The following strategies may be used in this class:

1. A review of the literature.
2. Check of the reading.
3. Analysis of assigned readings.
4. Group discussions.
5. Individual and group discussions.
6. Preparation of reports.
7. Preparation of a didactic plan.
8. Carrying out a micro-class.

### Instructional Materials and References

None

### Assessment Criteria and Methods of Evaluating Students

| Grade | Coefficient |
|-------|-------------|
| AA    | 4.00        |
| BA    | 3.50        |
| BB    | 3.00        |
| CB    | 2.50        |
| CC    | 2.00        |
| DC    | 1.50        |
| DD    | 1.00        |
| FF    | 0.00        |
| VF    | 0.00        |



| <b>Distribution of Grade Elements</b>                   |          |            |
|---|----------|------------|
| In-Term Studies   | Quantity | Percentage |
| Homework  | 1        | 30         |
| Midterm   | 1        | 30         |
|   |          |            |
| <b>Total</b>  |          | 60         |
| End-Term Studies  | Quantity | Percentage |
| Final Project   | 1        | 40         |
| <b>Total</b>  |          | 40         |
| <b>Contribution Of In-Term Studies To Overall Grade</b> |          | 60         |
| <b>End-Term Studies</b>                                 |          | 40         |
| <b>Total</b>  |          | 100        |

Date Syllabus Was Last Reviewed: September 2015