



| | |
|------------------|-------------|
| FORENAME SURNAME | |
| DEPARTMENT | STUDENT NO. |
| TEACHER | SIGNATURE |

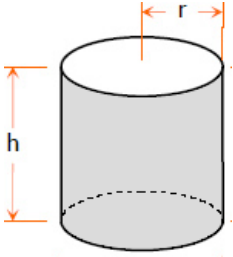
| | | | |
|-----|-----|-----|-------|
| 1 | 2 | 3 | TOTAL |
| /20 | /20 | /15 | |
| 4 | 5 | | |
| /20 | /25 | | /100 |

(You must show your working for all questions.)

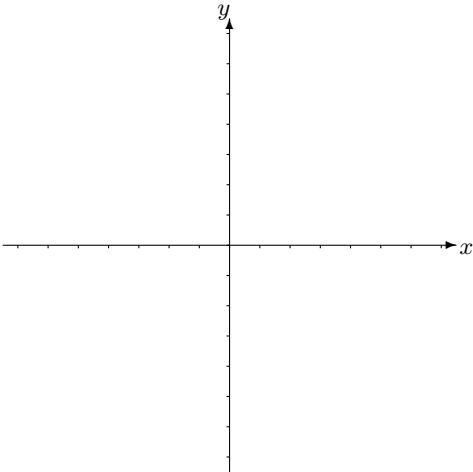
1. [20 pts] Find the lines that are (a) *tangent* and (b) *normal* to the curve $x \sin 2y = y \cos 2x$ at the point $(\pi/4, \pi/2)$.

[p154 q36]

3. [15 pts] What are the dimensions of the lightest (minimum surface area) open-top right circular cylindrical can that will hold a volume of 1000 cm^3 [p282 q35]



2. [20 pts] Find the area of the region enclosed by $y = x^2 - 2x$ and $y = x$. [p298 q44]



4. [20 pts] Find $F(4)$ and $F'(x)$ if

$$F(x) = \int_{\sqrt{x}}^2 \sin(t^2) dt$$

[p282 q35]

5. [25 pts] Suppose

$$y = \frac{8x}{x^2 + 4}, \quad y' = \frac{-8x^2 + 32}{(x^2 + 4)^2}, \quad \text{and} \quad y'' = \frac{16x(x^2 - 12)}{(x^2 + 4)^3}.$$

[p211 q43]

a) Determine where the graph of y is increasing and where it is decreasing. Find the local maxima or minima, if any.

| x | y' | y'' | y |
|------------------------|------|-------|-----|
| $-\infty < x < \cdots$ | | | |
| $\cdots < x < \cdots$ | | | |
| $\cdots < x < \cdots$ | | | |
| $\cdots < x < \cdots$ | | | |
| $\cdots < x < \cdots$ | | | |
| $\cdots < x < +\infty$ | | | |

b) Determine where the graph of y is concave up and where it is concave down. Find the inflection points, if any.

c) Sketch the curve on the given coordinate system.

