

Your Name / Ad - Soyad

(time:60)

Signature / İmza

Student ID # / Öğrenci No

(mavi tükenmez!)

| Problem | 1 | 2 | 3 | 4 | Total |
|---------|----|----|----|----|-------|
| Points: | 25 | 25 | 25 | 25 | 100 |
| Score: | | | | | |

1. (a) (13 Points) $\int \frac{9x^3 - 3x + 1}{x^3 - x^2} dx = ?$

(b) (12 Points) Evaluate the improper integral $\int_{-\infty}^{+\infty} 2xe^{-x^2} dx$.

2. (a) (12 Points) Suppose $a_n = \frac{\ln(n+1)}{\sqrt{n}}$. Does the sequence $\{a_n\}_{n=1}^{\infty}$ converge? If it converges, find its limit.

- (b) (13 Points) Find a formula for the n th partial sum s_n and find the sum of the series

$$\frac{1}{2 \cdot 3} + \frac{1}{3 \cdot 4} + \frac{1}{5 \cdot 6} + \cdots + \frac{1}{(n+1) \cdot (n+2)} + \cdots$$

3. (a) (12 Points) Does the series $\sum_{n=0}^{\infty} \frac{e^n}{e^n + n}$ converge or diverge? Name the test you use.

- (b) (13 Points) Does the series

$$\sum_{n=0}^{\infty} \left(\frac{1}{2^n} + \frac{(-1)^n}{5^n} \right)$$

converge? If it converges, find its sum.

4. (a) (13 Points) Determine if $\sum_{n=1}^{\infty} \frac{n2^n(n+1)!}{3^n n!}$ converges or diverges. Give reason.

(b) (12 Points) Determine if $\sum_{n=1}^{\infty} \frac{n+1}{n^2 \sqrt{n}}$ converges or diverges. Give reason.